

Matrices And Determinants

Subjects : Maths

Previous Year Questions of JEE
Mains

Maths - Section A (MCQ.)

1. Let $\alpha, \beta \in \mathbb{R}$ be such that the system of linear equations
- $$\begin{aligned}x + 2y + z &= 5 \\2x + y + \alpha z &= 5 \\8x + 4y + \beta z &= 18\end{aligned}$$
- has no solution. Then $\frac{\beta}{\alpha}$ is equal to :
- A) -4 B) 4 C) 8 D) -8
2. If the system of equations
- $$\begin{aligned}x + 5y + 6z &= 4, \\2x + 3y + 4z &= 7, \\x + 6y + az &= b\end{aligned}$$
- has infinitely many solutions, then the point (a, b) lies on the line
- A) $y - x = 3$ B) $x - y = 3$ C) $x + y = 11$ D) $x + y = 12$
3. Consider the system of linear equations in x, y, z :
- $$\begin{aligned}x + 2y + tz &= 0, \\6x + y + 5tz &= 0, \\3x + t^2y + f(t)z &= 0,\end{aligned}$$
- where $f : \mathbb{R} \rightarrow \mathbb{R}$ is a differentiable function. If this system has infinitely many solutions for all $t \in \mathbb{R}$, then f
- A) is a constant function B) is strictly increasing on $\mathbb{R}$
C) is strictly decreasing on $\mathbb{R}$ D) has two critical points
4. Let $A = \begin{bmatrix} 1 & 3 & -1 \\ 2 & 1 & \alpha \\ 0 & 1 & -1 \end{bmatrix}$ be a singular matrix. Let $f(x) = \int_0^x (t^2 + 2t + 3) dt$, $x \in [1, \alpha]$. If M and m are respectively the maximum and the minimum values of f in $[1, \alpha]$, then $3(M - m)$ is equal to :
- A) 64 B) 68 C) 72 D) 76
5. If $f : \mathbb{N} \rightarrow \mathbb{Z}$ is defined by
- $$f(n) = \begin{vmatrix} n & -1 & -5 \\ -2n^2 & 3(2k+1) & 2k+1 \\ -3n^3 & 3k(2k+1) & 3k(k+2)+1 \end{vmatrix}, k \in \mathbb{N},$$
- and $\sum_{n=1}^k f(n) = 98$, then k is equal to :
- A) 3 B) 4 C) 5 D) 6

6. The sum of all possible values of $\theta \in [0, 2\pi]$, for which the system of equations :

$$x \cos 3\theta - 8y - 12z = 0$$

$$x \cos 2\theta + 3y + 3z = 0$$

$$x + y + 3z = 0$$

has a non-trivial solution, is equal to :

- A) π B) 2π C) 3π D) 4π

7. If the system of linear equations:

$$x + y + z = 6,$$

$$x + 2y + 5z = 10,$$

$$2x + 3y + \lambda z = \mu$$

has infinitely many solutions, then the value of $\lambda + \mu$ equals:

- A) 12 B) 16 C) 22 D) 28

8. Consider the matrices $A = \begin{bmatrix} 2 & -2 \\ 4 & -2 \end{bmatrix}$ and $B = \begin{bmatrix} 3 & 9 \\ 1 & 3 \end{bmatrix}$. If matrices P and Q are such that $PA = B$ and $AQ = B$, then the absolute value of the sum of the diagonal elements of $2(P + Q)$ is _____.

- A) 35 B) 33 C) 34 D) 36

9. Let $S = \left\{ A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} : a, b, c, d \in \{0, 1, 2, 3, 4\} \text{ and } A^2 - 4A + 3I = 0 \right\}$ be a set of 2×2 matrixes. Then the number of matrixes in S , for which the sum of the diagonal elements is equal to 4, is:

- A) 20 B) 17 C) 21 D) 19

10. Let $A = \begin{bmatrix} 1 & 1 & 2 \\ -2 & 0 & 1 \\ 1 & 3 & 5 \end{bmatrix}$. Then the sum of all elements of the matrix $\text{adj}(\text{adj}(2(\text{adj}A)^{-1}))$ is equal to:

- A) 3 B) 4 C) -4 D) -3

11. Let $A = \begin{bmatrix} 1 & 2 & 7 \\ 4 & -2 & 8 \\ 3 & 8 & -7 \end{bmatrix}$ and $\det(A - \alpha I) = 0$, where α is a real number. If the largest possible value of α is p , then the circle $(x - p)^2 + (y - 2p)^2 = 320$, intersects the co-ordinate axes at

- A) 1 point B) 2 points C) 3 points D) 4 points

12. Let M be a 3×3 matrix such that $M \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}$, $M \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 2 \end{pmatrix}$ and $M \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} -1 \\ 1 \\ 1 \end{pmatrix}$. If $M \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1 \\ 7 \\ 11 \end{pmatrix}$, then $x + y + z$ equals :

- A) 4 B) 5 C) 7 D) 11

13. Let A be a 3×3 matrix such that $A^T \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 5 \\ 2 \\ 2 \end{bmatrix}$, $A^T \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \\ 1 \end{bmatrix}$, $A \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 3 \\ 4 \\ 4 \end{bmatrix}$ and $A \begin{bmatrix} 0 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 1 \\ 3 \\ 1 \end{bmatrix}$. If $\det(A) = 1$, then $\det(\text{adj}(A^2 + A))$ is equal to:

- A) 16 B) 25 C) 49 D) 64

14. Let $A = \begin{bmatrix} -1 & 1 & -1 \\ 1 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$ satisfy $A^2 + \alpha(\text{adj}(\text{adj}(A))) + \beta(\text{adj}(A)(\text{adj}(\text{adj}(A)))) = \begin{bmatrix} 2 & -2 & 2 \\ -2 & 0 & -1 \\ 0 & 0 & -1 \end{bmatrix}$ for some $\alpha, \beta \in \mathbb{R}$. Then $(\alpha - \beta)^2$ is equal to _____

- A) 1 B) 2 C) 3 D) 4

15. Let $A = \begin{bmatrix} 1 & 0 & 0 \\ 3 & 1 & 0 \\ 9 & 3 & 1 \end{bmatrix}$ and $B = [b_{ij}]$, $1 \leq i, j \leq 3$. If $B = A^{99} - I$, then the value of $\frac{b_{31} - b_{21}}{b_{32}}$ is :

A) 99

B) 199

C) 149

D) 159

16. Let $A = \begin{bmatrix} \alpha & 1 & 2 \\ 2 & 3 & 0 \\ 0 & 4 & 5 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -5\alpha & 0 \\ 0 & 4\alpha & -2\alpha \end{bmatrix} + \text{adj}(A)$. If $\det(B) = 66$, then $\det(\text{adj}(A))$ equals:

A) 289

B) 361

C) 441

D) 529

17. Let $A = \begin{bmatrix} 3 & -4 \\ 1 & -1 \end{bmatrix}$ and B be two matrices such that $A^{100} = 100B + I$. Then the sum of all the elements of B^{100} is ____.

A) 0

B) 100

C) 1

D) -1

18. The number of 3×2 matrices A, which can be formed using the elements of the set $\{-2, -1, 0, 1, 2\}$ such that the sum of all the diagonal elements of $A^T A$ is 5, is ____.

A) 300

B) 312

C) 324

D) 340

19. If the system of equations $3x + y + 4z = 3$, $2x + ay - z = -3$, $x + 2y + z = 4$ has no solution, then the value of a is equal to :

A) 19

B) 4

C) 13

D) 23

20. The system of linear equations

$$x + y + z = 6,$$

$$2x + 5y + az = 36,$$

$$x + 2y + 3z = b \text{ has:}$$

A) unique solution for $a = 8$ and $b = 16$ B) infinitely many solutions for $a = 8$ and $b = 14$ C) infinitely many solutions for $a = 8$ and $b = 16$ D) unique solution for $a = 8$ and $b = 14$

21. If $A = \begin{bmatrix} 2 & 3 \\ 3 & 5 \end{bmatrix}$, then the determinant of the matrix $(A^{2025} - 3A^{2024} + A^{2023})$ is

A) 28

B) 12

C) 24

D) 16

22. Let n be the number obtained on rolling a fair die. If the probability that the system

$$x - ny + z = 6$$

$$x + (n - 2)y + (n + 1)z = 8$$

$$(n - 1)y + z = 1$$

Has a unique solution is $\frac{k}{6}$, then the sum of k and all possible values of n is:

A) 21

B) 24

C) 20

D) 22

23. Let $A = \begin{bmatrix} 2 & 2+p & 2+p+q \\ 4 & 6+2p & 8+3p+2q \\ 6 & 12+3p & 20+6p+3q \end{bmatrix}$.

If $\det(\text{adj}(\text{adj}(3A))) = 2^m \cdot 3^n$, $m, n \in \mathbb{N}$, then $m + n$ is equal to

A) 22

B) 24

C) 26

D) 20

24. Let I be the identity matrix of order 3×3 and for the matrix $A = \begin{bmatrix} \lambda & 2 & 3 \\ 4 & 5 & 6 \\ 7 & -1 & 2 \end{bmatrix}$, $|A| = -1$. Let B be the inverse of the matrix $\text{adj}(A \text{adj}(A^2))$. Then $|(\lambda B + 1)|$ is equal to ____

A) 30

B) 32

C) 36

D) 38

25. Let A be a matrix of order 3×3 and $|A| = 5$. If $|2 \text{adj}(3A \text{adj}(2A))| = 2^\alpha \cdot 3^\beta \cdot 5^\gamma$, $\alpha, \beta, \gamma \in \mathbb{N}$ then $\alpha + \beta + \gamma$ is equal to

A) 25

B) 26

C) 27

D) 28

26. For a 3×3 matrix M , let $\text{trace}(M)$ denote the sum of all the diagonal elements of M . Let A be a 3×3 matrix such that $|A| = \frac{1}{2}$ and $\text{trace}(A) = 3$. If $B = \text{adj}(\text{adj}(2A))$, then the value of $|B| + \text{trace}(B)$ equals :

A) 56

B) 132

C) 174

D) 280

27. Let the system of equations

$$x + 5y - z = 1$$

$$4x + 3y - 3z = 7$$

$$24x + y + \lambda z = \mu$$

$\lambda, \mu \in \mathbb{R}$, have infinitely many solutions. Then the number of the solutions of this system, If x, y, z are integers and satisfy $7 \leq x + y + z \leq 77$, is

A) 3

B) 6

C) 5

D) 4

28. If the system of linear equations

$$3x + y + \beta z = 3$$

$$2x + \alpha y - z = -3$$

$$x + 2y + z = 4$$

has infinitely many solutions, then the value of $22\beta - 9\alpha$ is :

A) 49

B) 31

C) 43

D) 37

29. Let $A = \begin{bmatrix} \frac{1}{\sqrt{2}} & -2 \\ 0 & 1 \end{bmatrix}$ and $P = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}$, $\theta > 0$. If $B = PAP^T$, $C = P^T B^{10} P$ and the sum of the diagonal elements of C is $\frac{m}{n}$, where $\gcd(m, n) = 1$, then $m + n$ is :

A) 127

B) 258

C) 65

D) 2049

30. For some a, b , let $f(x) = \begin{vmatrix} a + \frac{\sin x}{x} & 1 & b \\ a & 1 + \frac{\sin x}{x} & b \\ a & 1 & b + \frac{\sin x}{x} \end{vmatrix}$, $x \neq 0$, $\lim_{x \rightarrow 0} f(x) = \lambda + \mu a + \nu b$. Then $(\lambda + \mu + \nu)^2$ is equal to :

A) 16

B) 25

C) 9

D) 36

31. The system of equations

$$x + y + z = 6$$

$$x + 2y + 5z = 9, \text{ has no solution if}$$

$$x + 5y + \lambda z = \mu,$$

A) $\lambda = 15, \mu \neq 17$ B) $\lambda \neq 17, \mu \neq 18$ C) $\lambda = 17, \mu \neq 18$ D) $\lambda = 17, \mu = 18$

32. If the system of equations

$$(\lambda - 1)x + (\lambda - 4)y + \lambda z = 5$$

$$\lambda x + (\lambda - 1)y + (\lambda - 4)z = 7$$

$$(\lambda + 1)x + (\lambda + 2)y - (\lambda + 2)z = 9$$

has infinitely many solutions, then $\lambda^2 + \lambda$ is equal to

A) 6

B) 10

C) 20

D) 12

33. Let $P = [p_{ij}]$ and $Q = [q_{ij}]$ be two square matrices of order 3 such that $q_{ij} = 2^{(i+j-1)} p_{ij}$ and $\det(Q) = 2^{10}$. Then the value of $\det(\text{adj}(\text{adj } P))$ is:

A) 32

B) 16

C) 81

D) 124

34. If $X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$ is a solution of the system of equations $AX = B$ where $\text{adj } A = \begin{bmatrix} 4 & 2 & 2 \\ -5 & 0 & 5 \\ 1 & -2 & 3 \end{bmatrix}$ and $B = \begin{bmatrix} 4 \\ 0 \\ 2 \end{bmatrix}$, then $|x + y + z|$ is equal to:

A) 3

B) $\frac{3}{2}$

C) 1

D) 2

35. Let $\alpha, \beta (\alpha \neq \beta)$ be the values of m , for which the equations $x + y + z = 1; x + 2y + 4z = m$ and $x + 4y + 10z = m^2$ have infinitely many solutions. Then the value of $\sum_{n=1}^{10} (n^\alpha + n^\beta)$ is equal to :
- A) 3080 B) 560 C) 3410 D) 440
36. Let M and m respectively be the maximum and the minimum values of
- $$f(x) = \begin{vmatrix} 1 + \sin^2 x & \cos^2 x & 4 \sin 4x \\ \sin^2 x & 1 + \cos^2 x & 4 \sin 4x \\ \sin^2 x & \cos^2 x & 1 + 4 \sin 4x \end{vmatrix}, x \in \mathbb{R}$$
- Then $M^4 - m^4$ is equal to :
- A) 1280 B) 1295 C) 1215 D) 1040

Maths - Section B (Numeric)

37. For some $\alpha, \beta \in \mathbb{R}$ let $A = \begin{bmatrix} \alpha & 2 \\ 1 & 2 \end{bmatrix}$ and $B = \begin{bmatrix} 1 & 1 \\ 1 & \beta \end{bmatrix}$ be such that $A^2 - 4A + 2I = B^2 - 3B + I = O$. Then $(\det(\text{adj}(A^3 - B^3)))^2$ is equal to
38. Let A be a 3×3 matrix such that $A + A^T = O$. If $A \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \\ 2 \end{bmatrix}$, $A^2 \begin{bmatrix} 1 \\ -1 \\ 0 \end{bmatrix} = \begin{bmatrix} -3 \\ 19 \\ -24 \end{bmatrix}$ and $\det(\text{adj}(2\text{adj}(A + I))) = (2)^\alpha \cdot (3)^\beta \cdot (11)^\gamma$, then $\alpha + \beta + \gamma$ is equal to ____.
39. Let $|A| = 6$ where A is a 3×3 matrix. If $|\text{adj}(3\text{adj}(A^2 \cdot \text{adj}(2A)))| = 2^m \cdot 3^n$, $m, n \in \mathbb{N}$, then $m + n$ is equal to:
40. Let A be a square matrix of order 3 such that $\det(A) = -2$ and $\det(3\text{adj}(-6\text{adj}(3A))) = 2^{m+n} \cdot 3^{mn}$, $m > n$. Then $4m + 2n$ is equal to _____

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Matrices And Determinants

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Previous Year Questions of JEE
Mains

Maths - Section A (MCQ.)

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11 - C	12 - B	13 - D	14 - D	15 - C	16 - C	17 - A	18 - B	19 - A	20 - B
21 - D	22 - D	23 - B	24 - D	25 - C	26 - D	27 - A	28 - B	29 - C	30 - A
31 - C	32 - D	33 - B	34 - D	35 - D	36 - A				

Maths - Section B (Numeric)

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