

Straight Lines

Subjects : Maths

Previous Year Questions

Maths - Section A (MCQ.)

- Let a circle pass through the origin and its centre be the point of intersection of two mutually perpendicular lines $x + (k - 1)y + 3 = 0$ and $2x + k^2y - 4 = 0$. If the line $x - y + 2 = 0$ intersects the circle at the points A and B, then $(AB)^2$ is equal to:
A) 10 B) 27 C) 18 D) 34
- Let the mid points of the sides of a triangle ABC be $\left(\frac{5}{2}, 7\right)$, $\left(\frac{5}{2}, 3\right)$ and $(4, 5)$. If its incentre is (h, k) , then $3h + k$ is equal to :
A) 11 B) 12 C) 13 D) 14
- Let the line $L_1 : x + 3 = 0$ intersect the lines $L_2 : x - y = 0$ and $L_3 : 3x + y = 0$ at the points A and B, respectively. Let the bisector of the obtuse angle between the lines L_2 and L_3 intersect the line L_1 at the point C. Then $BC^2 : AC^2$ is equal to:
A) 5 : 1 B) 1 : 5 C) 2 : 3 D) 3 : 2
- In an equilateral triangle PQR, let the vertex P be at $(3, 5)$ and the side QR be along the line $x + y = 4$. If the orthocentre of the triangle PQR is (α, β) , then $9(\alpha + \beta)$ is equal to:
A) 16 B) 27 C) 36 D) 48
- If a straight line drawn through the point of intersection of the lines $4x + 3y - 1 = 0$ and $3x + 4y - 1 = 0$, meets the co-ordinate axes at the points P and Q, then the locus of the mid point of PQ is:
A) $x + y - 7 = 0$ B) $x + y - 14xy = 0$ C) $2x + y + 14xy = 0$ D) $x + 2y - 14xy = 0$
- Let ABC be an equilateral triangle with orthocenter at the origin and the side BC on the line $x + 2\sqrt{2}y = 4$. If the co-ordinates of the vertex A are (α, β) , then the greatest integer less than or equal to $|\alpha + \sqrt{2}\beta|$ is
A) 2 B) 3 C) 5 D) 4
- Let $A(1, 0)$, $B(2, -1)$ and $C(\frac{7}{3}, \frac{4}{3})$ be three points. If the equation of the bisector of the angle ABC is $\alpha x + \beta y = 5$, then the value of $\alpha^2 + \beta^2$ is
A) 8 B) 5 C) 13 D) 10
- Let the angles made with the positive x-axis by two straight lines drawn from the point $P(2, 3)$ and meeting the line $x + y = 6$ at a distance $\sqrt{\frac{2}{3}}$ from the point P be θ_1 and θ_2 . Then the value of $(\theta_1 + \theta_2)$ is:
A) $\frac{\pi}{12}$ B) $\frac{\pi}{6}$ C) $\frac{\pi}{2}$ D) $\frac{\pi}{3}$
- Let $A(1, 2)$ and $C(-3, -6)$ be two diagonally opposite vertices of a rhombus, whose sides AD and BC are parallel to the line $7x - y = 14$. If $B(\alpha, \beta)$ and $D(\gamma, \delta)$ are the other two vertices, then $|\alpha + \beta + \gamma + \delta|$ is equal to:
A) 9 B) 3 C) 6 D) 1

10. A rectangle is formed by the lines $x = 0, x = 3, y = 0$ and $y = 4$. Let the line L be perpendicular to $3x + y + 6 = 0$ and divide the area of the rectangle into two equal parts. Then the distance of the point $(\frac{1}{2}, -5)$ from the line L is equal to:
- A) $2\sqrt{5}$ B) $3\sqrt{10}$ C) $\sqrt{10}$ D) $2\sqrt{10}$
11. Let a point A lie between the parallel lines L_1 and L_2 such that its distances from L_1 and L_2 are 6 and 3 units, respectively. Then the area (in sq. units) of the equilateral triangle ABC , where the points B and C lie on the lines L_1 and L_2 respectively, is:
- A) $15\sqrt{6}$ B) 27 C) $21\sqrt{3}$ D) $12\sqrt{2}$
12. A line passing through the point $P(a, 0)$ makes an acute angle α with the positive x -axis. Let this line be rotated about the point P through an angle $\frac{\alpha}{2}$ in the clock-wise direction. If in the new position, the slope of the line is $2 - \sqrt{3}$ and its distance from the origin is $\frac{1}{\sqrt{2}}$, then the value of $3a^2 \tan^2 \alpha - 2\sqrt{3}$ is
- A) 4 B) 6 C) 5 D) 8
13. Let the three sides of a triangle are on the lines $4x - 7y + 10 = 0, x + y = 5$ and $7x + 4y = 15$. Then the distance of its orthocentre from the orthocentre of the triangle formed by the lines $x = 0, y = 0$ and $x + y = 1$ is
- A) 5 B) $\sqrt{5}$ C) $\sqrt{20}$ D) 20
14. Let a be the length of a side of a square $OABC$ with O being the origin. Its side OA makes an acute angle α with the positive x -axis and the equations of its diagonals are $(\sqrt{3} + 1)x + (\sqrt{3} - 1)y = 0$ and $(\sqrt{3} - 1)x - (\sqrt{3} + 1)y + 8\sqrt{3} = 0$. Then a^2 is equal to
- A) 48 B) 32 C) 16 D) 24
15. If the orthocentre of the triangle formed by the lines $y = x + 1, y = 4x - 8$ and $y = mx + c$ is at $(3, -1)$, then $m - c$ is:
- A) 0 B) -2 C) 4 D) 2
16. Let ABC be the triangle such that the equations of lines AB and AC be $3y - x = 2$ and $x + y = 2$, respectively, and the points B and C lie on x -axis. If P is the orthocentre of the triangle ABC , then the area of the triangle PBC is equal to
- A) 4 B) 10 C) 8 D) 6
17. Let A and B be two distinct points on the line $L : \frac{x-6}{3} = \frac{y-7}{2} = \frac{z-7}{-2}$. Both A and B are at a distance $2\sqrt{17}$ from the foot of perpendicular drawn from the point $(1, 2, 3)$ on the line L . If O is the origin, then $\vec{OA} \cdot \vec{OB}$ is equal to:
- A) 49 B) 47 C) 21 D) 62
18. Let $ABCD$ be a tetrahedron such that the edges AB, AC and AD are mutually perpendicular. Let the areas of the triangles ABC, ACD and ADB be 5, 6 and 7 square units respectively. Then the area (in square units) of the $\triangle BCD$ is equal to:
- A) $\sqrt{340}$ B) 12 C) $\sqrt{110}$ D) $7\sqrt{3}$
19. Let the line $x + y = 1$ meet the axes of x and y at A and B , respectively. A right angled triangle AMN is inscribed in the triangle OAB , where O is the origin and the points M and N lie on the lines OB and AB , respectively. If the area of the triangle AMN is $\frac{4}{9}$ of the area of the triangle OAB and $AN : NB = \lambda : 1$, then the sum of all possible value(s) of λ is:
- A) 2 B) $\frac{5}{2}$ C) $\frac{1}{2}$ D) $\frac{13}{6}$
20. Let ABC be a triangle formed by the lines $7x - 6y + 3 = 0, x + 2y - 31 = 0$ and $9x - 2y - 19 = 0$. Let the point (h, k) be the image of the centroid of $\triangle ABC$ in the line $3x + 6y - 53 = 0$. Then $h^2 + k^2 + hk$ is equal to:

A) 47

B) 37

C) 36

D) 40

21. Let ${}^nC_{r-1} = 28$, ${}^nC_r = 56$ and ${}^nC_{r+1} = 70$. Let $A(4 \cos t, 4 \sin t)$, $B(2 \sin t, -2 \cos t)$ and $C(3r - n, r^2 - n - 1)$ be the vertices of a triangle ABC , where t is a parameter. If $(3x - 1)^2 + (3y)^2 = \alpha$, is the locus of the centroid of triangle ABC , then α equals
- A) 6 B) 18 C) 8 D) 20
22. Let the points $(\frac{11}{2}, \alpha)$ lie on or inside the triangle with sides $x + y = 11$, $x + 2y = 16$ and $2x + 3y = 29$. Then the product of the smallest and the largest values of α is equal to :
- A) 44 B) 22 C) 33 D) 55
23. A rod of length eight units moves such that its ends A and B always lie on the lines $x - y + 2 = 0$ and $y + 2 = 0$, respectively. If the locus of the point P , that divides the rod AB internally in the ratio $2 : 1$ is $9(x^2 + \alpha y^2 + \beta xy + \gamma x + 28y) - 76 = 0$, then $\alpha - \beta - \gamma$ is equal to :
- A) 22 B) 21 C) 23 D) 24
24. Let the area of a $\triangle PQR$ with vertices $P(5, 4)$, $Q(-2, 4)$ and $R(a, b)$ be 35 square units. If its orthocenter and centroid are $O(2, \frac{14}{5})$ and $C(c, d)$ respectively, then $c + 2d$ is equal to
- A) $\frac{8}{3}$ B) $\frac{7}{3}$ C) 2 D) 3
25. Let the triangle PQR be the image of the triangle with vertices $(1, 3)$, $(3, 1)$ and $(2, 4)$ in the line $x + 2y = 2$. If the centroid of $\triangle PQR$ is the point (α, β) , then $15(\alpha - \beta)$ is equal to :
- A) 19 B) 24 C) 21 D) 22
26. Consider the lines $x(3\lambda + 1) + y(7\lambda + 2) = 17\lambda + 5$, λ being a parameter, all passing through a point P . One of these lines (say L) is farthest from the origin. If the distance of L from the point $(3, 6)$ is d , then the value of d^2 is
- A) 20 B) 30 C) 10 D) 15
27. Let the lines $3x - 4y - \alpha = 0$, $8x - 11y - 33 = 0$, and $2x - 3y + \lambda = 0$ be concurrent. If the image of the point $(1, 2)$ in the line $2x - 3y + \lambda = 0$ is $(\frac{57}{13}, \frac{-40}{13})$, then $|\alpha\lambda|$ is equal to
- A) 84 B) 113 C) 91 D) 101
28. Let the equation $x(x + 2)(12 - k) = 2$ have equal roots. Then the distance of the point $(k, \frac{k}{2})$ from the line $3x + 4y + 5 = 0$ is
- A) 15 B) $5\sqrt{3}$ C) $15\sqrt{5}$ D) 12
29. Let the range of the function $f(x) = 6 + 16 \cos x \cdot \cos(\frac{\pi}{3} - x) \cdot \cos(\frac{\pi}{3} + x) \cdot \sin 3x \cdot \cos 6x$, $x \in \mathbf{R}$ be $[\alpha, \beta]$. Then the distance of the point (α, β) from the line $3x + 4y + 12 = 0$ is :
- A) 11 B) 8 C) 10 D) 9
30. If for $\theta \in [-\frac{\pi}{3}, 0]$, the points $(x, y) = (3 \tan(\theta + \frac{\pi}{3}), 2 \tan(\theta + \frac{\pi}{6}))$ lie on $xy + \alpha x + \beta y + \gamma = 0$, then $\alpha^2 + \beta^2 + \gamma^2$ is equal to :
- A) 80 B) 72 C) 96 D) 75
31. A line passes through the origin and makes equal angles with the positive coordinate axes. It intersects the lines $L_1 : 2x + y + 6 = 0$ and $L_2 : 4x + 2y - p = 0$, $p > 0$, at the points A and B , respectively. If $AB = \frac{9}{\sqrt{2}}$ and the foot of the perpendicular from the point A on the line L_2 is M , then $\frac{AM}{BM}$ is equal to
- A) 5 B) 4 C) 2 D) 3
32. Two equal sides of an isosceles triangle are along $-x + 2y = 4$ and $x + y = 4$. If m is the slope of its third side, then the sum, of all possible distinct values of m , is :

A) $-2\sqrt{10}$

B) 12

C) 6

D) -6

33. Let the area of the triangle formed by a straight Line L: $x + by + c = 0$ with co-ordinate axes be 48 square units. If the perpendicular drawn from the origin to the line L makes an angle of 45° with the positive x - axis, then the value of $b^2 + c^2$ is:
- A) 90 B) 93 C) 97 D) 83
34. Two vertices of a triangle ABC are $A(3, -1)$ and $B(-2, 3)$, and its orthocentre is $P(1, 1)$. If the coordinates of the point C are (α, β) and the centre of the circle circumscribing the triangle PAB is (h, k) , then the value of $(\alpha + \beta) + 2(h + k)$ equals :
- A) 51 B) 81 C) 5 D) 15
35. A variable line L passes through the point $(3, 5)$ and intersects the positive coordinate axes at the points A and B. The minimum area of the triangle OAB, where O is the origin, is :
- A) 30 B) 25 C) 40 D) 35
36. A ray of light coming from the point $P(1, 2)$ gets reflected from the point Q on the x-axis and then passes through the point $R(4, 3)$. If the point $S(h, k)$ is such that PQRS is a parallelogram, then hk^2 is equal to
- A) 80 B) 90 C) 60 D) 70
37. If the line segment joining the points $(5, 2)$ and $(2, a)$ subtends an angle $\frac{\pi}{4}$ at the origin, then the absolute value of the product of all possible values of a is:
- A) 6 B) 8 C) 2 D) 4
38. If the image of the point $(-4, 5)$ in the line $x + 2y = 2$ lies on the circle $(x + 4)^2 + (y - 3)^2 = r^2$, then r is equal to:
- A) 1 B) 2 C) 4 D) 3
39. The equations of two sides AB and AC of a triangle ABC are $4x + y = 14$ and $3x - 2y = 5$, respectively. The point $(2, -\frac{4}{3})$ divides the third side BC internally in the ratio 2 : 1. The equation of the side BC is :
- A) $x - 6y - 10 = 0$ B) $x - 3y - 6 = 0$ C) $x + 3y + 2 = 0$ D) $x + 6y + 6 = 0$
40. If the locus of the point, whose distances from the point $(2, 1)$ and $(1, 3)$ are in the ratio 5 : 4, is $ax^2 + by^2 + cxy + dx + ey + 170 = 0$, then the value of $a^2 + 2b + 3c + 4d + e$ is equal to :
- A) 5 B) -27 C) 37 D) 437
41. A circle is inscribed in an equilateral triangle of side of length 12. If the area and perimeter of any square inscribed in this circle are m and n , respectively, then $m + n^2$ is equal to
- A) 396 B) 408 C) 312 D) 414
42. Let a variable line of slope $m > 0$ passing through the point $(4, -9)$ intersect the coordinate axes at the points A and B. the minimum value of the sum of the distances of A and B from the origin is
- A) 25 B) 30 C) 15 D) 10
43. Let two straight lines drawn from the origin O intersect the line $3x + 4y = 12$ at the points P and Q such that $\triangle OPQ$ is an isosceles triangle and $\angle POQ = 90^\circ$. If $l = OP^2 + PQ^2 + QO^2$, then the greatest integer less than or equal to l is :
- A) 44 B) 48 C) 46 D) 42
44. The equation of one of the straight lines which passes through the point $(1, 3)$ and makes an angle $\tan^{-1}(\sqrt{2})$ with the straight line, $y + 1 = 3\sqrt{2}x$ is
- A) $4\sqrt{2}x + 5y - (15 + 4\sqrt{2}) = 0$ B) $5\sqrt{2}x + 4y - (15 + 4\sqrt{2}) = 0$
- C) $4\sqrt{2}x + 5y - 4\sqrt{2} = 0$ D) $4\sqrt{2}x - 5y - (5 + 4\sqrt{2}) = 0$

45. Let ABC be a triangle with $A(-3, 1)$ and $\angle ACB = \theta$, $0 < \theta < \frac{\pi}{2}$. If the equation of the median through B is $2x + y - 3 = 0$ and the equation of angle bisector of C is $7x - 4y - 1 = 0$ then $\tan \theta$ is equal to:
- A) $\frac{1}{2}$ B) $\frac{3}{4}$ C) $\frac{4}{3}$ D) 2
46. Let A be a fixed point $(0, 6)$ and B be a moving point $(2t, 0)$. Let M be the mid-point of AB and the perpendicular bisector of AB meets the y -axis at C . The locus of the mid-point P of MC is :
- A) $3x^2 - 2y - 6 = 0$ B) $3x^2 + 2y - 6 = 0$ C) $2x^2 + 3y - 9 = 0$ D) $2x^2 - 3y + 9 = 0$
47. The vertices of a triangle are $A(-1, 3)$, $B(-2, 2)$ and $C(3, -1)$. A new triangle is formed by shifting the sides of the triangle by one unit inwards. Then the equation of the side of the new triangle nearest to origin is :
- A) $x - y - (2 + \sqrt{2}) = 0$ B) $-x + y - (2 - \sqrt{2}) = 0$
 C) $x + y - (2 - \sqrt{2}) = 0$ D) $x + y + (2 - \sqrt{2}) = 0$
48. Let $A(a, b)$, $B(3, 4)$ and $(-6, -8)$ respectively denote the centroid, circumcentre and orthocentre of a triangle. Then, the distance of the point $P(2a + 3, 7b + 5)$ from the line $2x + 3y - 4 = 0$ measured parallel to the line $x - 2y - 1 = 0$ is
- A) $\frac{15\sqrt{5}}{7}$ B) $\frac{17\sqrt{5}}{6}$ C) $\frac{17\sqrt{5}}{7}$ D) $\frac{\sqrt{5}}{17}$
49. Let $\alpha, \beta, \gamma, \delta \in \mathbb{Z}$ and let $A(\alpha, \beta)$, $B(1, 0)$, $C(\gamma, \delta)$ and $D(1, 2)$ be the vertices of a parallelogram $ABCD$. If $AB = \sqrt{10}$ and the points A and C lie on the line $3y = 2x + 1$, then $2(\alpha + \beta + \gamma + \delta)$ is equal to
- A) 10 B) 5 C) 12 D) 8
50. If $x^2 - y^2 + 2hxy + 2gx + 2fy + c = 0$ is the locus of a point, which moves such that it is always equidistant from the lines $x + 2y + 7 = 0$ and $2x - y + 8 = 0$, then the value of $g + c + h - f$ equals
- A) 14 B) 6 C) 8 D) 29
51. A line passing through the point $A(9, 0)$ makes an angle of 30° with the positive direction of x -axis. If this line is rotated about A through an angle of 15° in the clockwise direction, then its equation in the new position is
- A) $\frac{y}{\sqrt{3}-2} + x = 9$ B) $\frac{x}{\sqrt{3}-2} + y = 9$ C) $\frac{x}{\sqrt{3}+2} + y = 9$ D) $\frac{y}{\sqrt{3}+2} + x = 9$
52. Let A be the point of intersection of the lines $3x + 2y = 14$, $5x - y = 6$ and B be the point of intersection of the lines $4x + 3y = 8$, $6x + y = 5$. The distance of the point $P(5, -2)$ from the line AB is
- A) $\frac{13}{2}$ B) 8 C) $\frac{5}{2}$ D) 6
53. The distance of the point $(2, 3)$ from the line $2x - 3y + 28 = 0$, measured parallel to the line $\sqrt{3}x - y + 1 = 0$, is equal to
- A) $4\sqrt{2}$ B) $6\sqrt{3}$ C) $3 + 4\sqrt{2}$ D) $4 + 6\sqrt{3}$
54. In a $\triangle ABC$, suppose $y = x$ is the equation of the bisector of the angle B and the equation of the side AC is $2x - y = 2$. If $2AB = BC$ and the point A and B are respectively $(4, 6)$ and (α, β) , then $\alpha + 2\beta$ is equal to
- A) 42 B) 39 C) 48 D) 45
55. The portion of the line $4x + 5y = 20$ in the first quadrant is trisected by the lines L_1 and L_2 passing through the origin. The tangent of an angle between the lines L_1 and L_2 is:
- A) $\frac{8}{5}$ B) $\frac{25}{41}$ C) $\frac{2}{5}$ D) $\frac{30}{41}$
56. The equations of the sides AB , BC & CA of a triangle ABC are $2x + y = 0$, $x + py = 21a$ ($a \neq 0$) and $x - y = 3$ respectively. Let $P(2, a)$ be the centroid of the triangle ABC , then $(BC)^2$ is equal to
- A) 121 B) 122 C) 123 D) 124

57. Let a rectangle $ABCD$ of sides 2 and 4 be inscribed in another rectangle $PQRS$ such that the vertices of the rectangle $ABCD$ lie on the sides of the rectangle $PQRS$. Let a and b be the sides of the rectangle $PQRS$ when its area is maximum. Then $(a + b)^2$ is equal to :
- A) 72 B) 60 C) 80 D) 64
58. If the line, $2x - y + 3 = 0$ is at a distance $\frac{1}{\sqrt{5}}$ and $\frac{2}{\sqrt{5}}$ from the lines $4x - 2y + \alpha = 0$ and $6x - 3y + \beta = 0$, respectively, then the sum of all possible values of α and β is
- A) 12 B) 30 C) 18 D) 60

Maths - Section B (Numeric)

59. From the point $(-1, -1)$, two rays are sent making angles of 45° with the line $x + y = 0$. These rays get reflected from the mirror $x + 2y = 1$. If the equations of the reflected rays are $ax + by = 9$ and $cx + dy = 7$, $a, b, c, d \in \mathbf{Z}$, then the value of $ad + bc$ is _____.
60. If P is a point on the circle $x^2 + y^2 = 4$, Q is a point on the straight line $5x + y + 2 = 0$ and $x - y + 1 = 0$ is the perpendicular bisector of PQ, then 13 times the sum of abscissa of all such point P is
61. Let $A(4, -2), B(1, 1)$ and $C(9, -3)$ be the vertices of a triangle ABC . Then the maximum area of the parallelogram AFDE, formed with vertices D, E and F on the sides BC, CA and AB of the triangle ABC respectively, is _____ .
62. Let a ray of light passing through the point $(3, 10)$ reflects on the line $2x + y = 6$ and the reflected ray passes through the point $(7, 2)$. If the equation of the incident ray is $ax + by + 1 = 0$, then $a^2 + b^2 + 3ab$ is equal to
63. Consider a triangle ABC having the vertices $A(1, 2), B(\alpha, \beta)$ and $C(\gamma, \delta)$ and angles $\angle ABC = \frac{\pi}{6}$ and $\angle BAC = \frac{2\pi}{3}$. If the points B and C lie on the line $y = x + 4$, then $\alpha^2 + \gamma^2$ is equal to
64. Let ABC be an isosceles triangle in which A is at $(-1, 0)$, $\angle A = \frac{2\pi}{3}$, $AB = AC$ and B is on the positive x-axis. If $BC = 4\sqrt{3}$ and the line BC intersects the line $y = x + 3$ at (α, β) , then $\frac{\beta^4}{\alpha^2}$ is :
65. Let $A(-2, -1), B(1, 0), C(\alpha, \beta)$ and $D(\gamma, \delta)$ be the vertices of a parallelogram ABCD. If the point C lies on $2x - y = 5$ and the point D lies on $3x - 2y = 6$, then the value of $|\alpha + \beta + \gamma + \delta|$ is equal to

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Straight Lines

Subjects : Maths

Previous Year Questions

Maths - Section A (MCQ.)

1 - C	2 - C	3 - A	4 - D	5 - B	6 - D	7 - D	8 - C	9 - C	10 - D
11 - C	12 - A	13 - B	14 - A	15 - A	16 - D	17 - B	18 - C	19 - A	20 - B
21 - D	22 - C	23 - C	24 - D	25 - D	26 - A	27 - C	28 - A	29 - A	30 - D
31 - D	32 - C	33 - C	34 - C	35 - A	36 - D	37 - D	38 - B	39 - C	40 - C
41 - B	42 - A	43 - C	44 - A	45 - C	46 - C	47 - C	48 - C	49 - D	50 - A
51 - A	52 - D	53 - D	54 - A	55 - D	56 - B	57 - A	58 - B		

Maths - Section B (Numeric)

59 - 7	60 - 2	61 - 3	62 - 1	63 - 14	64 - 36	65 - 32
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